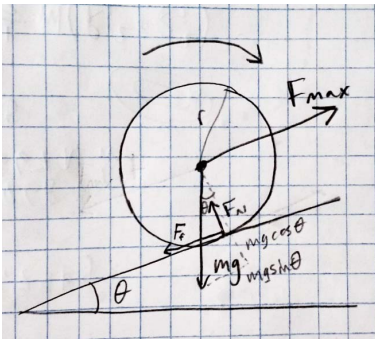
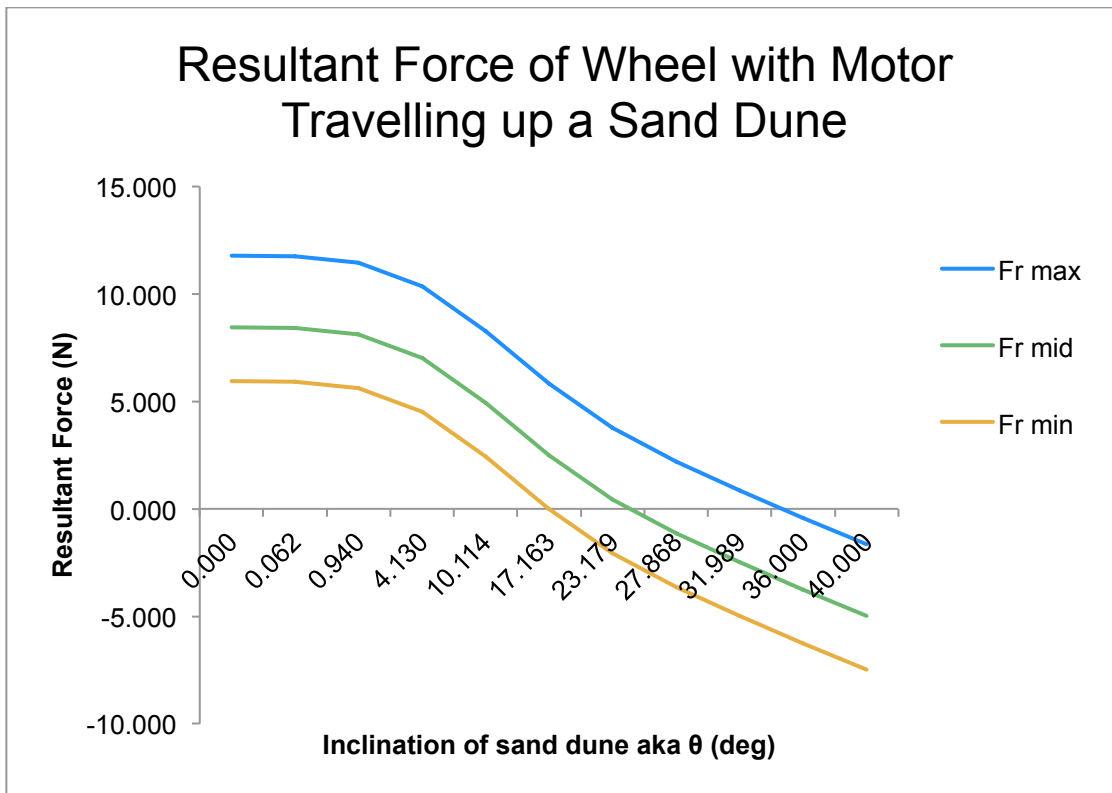


Motor Force V1.1 – Sept. 26, 2016



name	parameter	unit	value	expression
rated motor torque	T	N m	0.4002	specs from datasheet
scale factor motor torque	k	/	0.6	closer to reality
inner radius of wheel	r1	m	0.0475	
outer radius of wheel	r2	m	0.0550	
radius of wheel	r	m	0.0550	
mass robot total	mtotal	kg	2	
mass wheel	m	kg	0.500	
angle of incline	$\theta$	deg	10	
angle of incline radians	$\theta_{rad}$	rad	0.175	
sand static friction	us	/	0.850	uninformed estimate
sand kinetic friction	uk	/	0.700	uninformed estimate
max speed on grass	vgrass	m/s	0.130	from gps measurements
time to reach max speed	taccel	s	3	observation
acceleration on grass	agress	m/s <sup>2</sup>	0.0433	
gravity	g	m/s <sup>2</sup>	9.81	
force of motor	Fm	N	0.1374	$F_m = r/T$
moment of inertia for wheel	I	kg m <sup>2</sup>	0.0013 2	$I = (1/2)m(r_1^2 + r_2^2)$
acceleration from torque	a	m/s <sup>2</sup>	16.671	$a = (T*r)/I$
force maximum	Fmax	N	11.717	$F_{max} = ma + (mg*cos\theta*uk)$
force to overcome	Fo	N	3.407	$F_o = m_{total}*g*sin\theta$
force resultant	Fr	N	8.310	$F_{max}-F_o$
will wheel slip?	1 = yes, 0 = no	/	0	if $F_r < 1$ , then yes it will slip
sense of scale	s	kg	1.19	$F_{max}/g$

## Resultant Force of Wheel with Motor Travelling up a Sand Dune



robot motor force (N)			
	Fmax	Fo	Fr
1	<b>3.661</b>	<b>0.342</b>	<b>3.319</b>
2	<b>27.419</b>	<b>12.611</b>	<b>14.808</b>
3	10.367	1.710	8.657
4	10.200	5.078	5.122
5	8.628	9.810	-1.182
avg	12.055	5.910	6.145

### calculations

$$F_{net} = ma$$

$$F_{max} - F_f = ma$$

$$F_{max} = ma + (mg \cdot \cos\theta \cdot \mu_k)$$

$$\Sigma T = T_{net}$$

$$T = I \cdot \alpha$$

$$\alpha = (a/r)$$

$$T = I \cdot (a/r)$$

$$a = (T \cdot r) / I$$

**scenario 1: global min**

name	parameter	unit	value
rated motor torque	T	N m	0.1334
scale factor motor torque	k	/	0.2
inner radius of wheel	r1	m	0.0475
outer radius of wheel	r2	m	0.0550
radius of wheel	r	m	0.0550
mass robot total	mtotal	kg	2
mass wheel	m	kg	0.300
angle of incline	$\theta$	deg	1
angle of incline radians	$\theta_{rad}$	rad	0.017
sand static friction	$\mu_s$	/	0.850
sand kinetic friction	$\mu_k$	/	0.300
max speed on grass	vgrass	m/s	0.130
time to reach max speed	taccel	s	3
acceleration on grass	agress	m/s <sup>2</sup>	0.0433
gravity	g	m/s <sup>2</sup>	9.81
force of motor	Fm	N	0.4123
moment of inertia for wheel	I	kg m <sup>2</sup>	0.00079
acceleration from torque	a	m/s <sup>2</sup>	9.262
force maximum	Fmax	N	3.661
force to overcome	Fo	N	0.342
force resultant	Fr	N	3.319
will wheel slip?	1 = yes, 0 = no	/	0
sense of scale	s	kg	0.37

**scenario 2: global max**

name	parameter	unit	value
rated motor torque	T	N m	0.667
scale factor motor torque	k	/	1
inner radius of wheel	r1	m	0.0475
outer radius of wheel	r2	m	0.0550
radius of wheel	r	m	0.0550
mass robot total	mtotal	kg	2
mass wheel	m	kg	2.000
angle of incline	$\theta$	deg	40
angle of incline radians	$\theta_{rad}$	rad	0.698
sand static friction	$\mu_s$	/	0.850
sand kinetic friction	$\mu_k$	/	0.900
max speed on grass	vgrass	m/s	0.130
time to reach max speed	taccel	s	3

acceleration on grass	agrass	m/s <sup>2</sup>	0.0433
gravity	g	m/s <sup>2</sup>	9.81
force of motor	F <sub>m</sub>	N	0.0825
moment of inertia for wheel	I	kg m <sup>2</sup>	0.00528
acceleration from torque	a	m/s <sup>2</sup>	6.946
force maximum	F <sub>max</sub>	N	27.419
force to overcome	F <sub>o</sub>	N	12.611
force resultant	F <sub>r</sub>	N	14.808
will wheel slip?	1 = yes, 0 = no	/	0
sense of scale	s	kg	2.80

### scenario 3: rolling along the beach

name	parameter	unit	value
rated motor torque	T	N m	0.3335
scale factor motor torque	k	/	0.5
inner radius of wheel	r <sub>1</sub>	m	0.0475
outer radius of wheel	r <sub>2</sub>	m	0.0550
radius of wheel	r	m	0.0550
mass robot total	m <sub>total</sub>	kg	2
mass wheel	m	kg	0.500
angle of incline	θ	deg	5
angle of incline radians	θ <sub>rad</sub>	rad	0.087
sand static friction	μ <sub>s</sub>	/	0.850
sand kinetic friction	μ <sub>k</sub>	/	0.700
max speed on grass	v <sub>grass</sub>	m/s	0.130
time to reach max speed	t <sub>accel</sub>	s	3
acceleration on grass	agrass	m/s <sup>2</sup>	0.0433
gravity	g	m/s <sup>2</sup>	9.81
force of motor	F <sub>m</sub>	N	0.1649
moment of inertia for wheel	I	kg m <sup>2</sup>	0.00132
acceleration from torque	a	m/s <sup>2</sup>	13.893
force maximum	F <sub>max</sub>	N	10.367
force to overcome	F <sub>o</sub>	N	1.710
force resultant	F <sub>r</sub>	N	8.657
will wheel slip?	1 = yes, 0 = no	/	0
sense of scale	s	kg	1.06

### scenario 4: carrying a payload in front up a small hill

name	parameter	unit	value
rated motor torque	T	N m	0.2668
scale factor motor torque	k	/	0.4

inner radius of wheel	r1	m	0.0475
outer radius of wheel	r2	m	0.0550
radius of wheel	r	m	0.0550
mass robot total	mtotal	kg	2
mass wheel	m	kg	0.700
angle of incline	$\theta$	deg	15
angle of incline radians	$\theta_{rad}$	rad	0.262
sand static friction	us	/	0.850
sand kinetic friction	uk	/	0.700
max speed on grass	vgrass	m/s	0.130
time to reach max speed	taccel	s	3
acceleration on grass	agress	m/s <sup>2</sup>	0.0433
gravity	g	m/s <sup>2</sup>	9.81
force of motor	Fm	N	0.2061
moment of inertia for wheel	I	kg m <sup>2</sup>	0.00185
acceleration from torque	a	m/s <sup>2</sup>	7.939
force maximum	Fmax	N	10.200
force to overcome	Fo	N	5.078
force resultant	Fr	N	5.122
will wheel slip?	1 = yes, 0 = no	/	0
sense of scale	s	kg	1.04

### scenario 5: traversing up a mini sand dune with a payload in front

name	parameter	unit	value
rated motor torque	T	N m	0.2001
scale factor motor torque	k	/	0.3
inner radius of wheel	r1	m	0.0475
outer radius of wheel	r2	m	0.0550
radius of wheel	r	m	0.0550
mass robot total	mtotal	kg	2
mass wheel	m	kg	0.750
angle of incline	$\theta$	deg	30
angle of incline radians	$\theta_{rad}$	rad	0.524
sand static friction	us	/	0.850
sand kinetic friction	uk	/	0.700
max speed on grass	vgrass	m/s	0.130
time to reach max speed	taccel	s	3
acceleration on grass	agress	m/s <sup>2</sup>	0.0433
gravity	g	m/s <sup>2</sup>	9.81
force of motor	Fm	N	0.2749
moment of inertia for wheel	I	kg m <sup>2</sup>	0.00198
acceleration from torque	a	m/s <sup>2</sup>	5.557

force maximum	$F_{max}$	N	8.628
force to overcome	$F_o$	N	9.810
force resultant	$F_r$	N	-1.182
will wheel slip?	1 = yes, 0 = no	/	1
sense of scale	s	kg	0.88